

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag                          | matrix (polar)  | det | TR |
|-----|------------------------------|---|-----|----|
| 1   | $\{1 0\}$                    | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$             | 1   | 1  |
| 2   | $\{2_{001} 0\}$              | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$           | 1   | 1  |
| 3   | $\{m_{110} 00\frac{1}{2}\}$  | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | -1  | 1  |
| 4   | $\{m_{1-10} 00\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$   | -1  | 1  |
| 5   | $\{4_{001}^+ '0\}$           | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$            | 1   | -1 |
| 6   | $\{4_{001}^- '0\}$           | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$            | 1   | -1 |
| 7   | $\{m_{100}' 00\frac{1}{2}\}$ | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$  | -1  | -1 |
| 8   | $\{m_{010}' 00\frac{1}{2}\}$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$  | -1  | -1 |