

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag                           | matrix (polar)  | det | TR |
|-----|-------------------------------|---|-----|----|
| 1   | $\{1 0\}$                     | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$             | 1   | 1  |
| 2   | $\{4_{001}^+ 00\frac{1}{2}\}$ | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$  | 1   | 1  |
| 3   | $\{4_{001}^- 00\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$  | 1   | 1  |
| 4   | $\{2_{001} 0\}$               | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$           | 1   | 1  |
| 5   | $\{m_{100}' 0\}$              | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$            | -1  | -1 |
| 6   | $\{m_{010}' 0\}$              | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$            | -1  | -1 |
| 7   | $\{m_{110}' 00\frac{1}{2}\}$  | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | -1  | -1 |
| 8   | $\{m_{1-10}' 00\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$   | -1  | -1 |