

PG No. 7 C_{2v} $mm2$ [orthorhombic] (axial, internal polar quadrupole)

* Harmonics for rank 0

* Harmonics for rank 1

$$\vec{G}_1^{(2,1)}[q](A_2)$$

** symmetry

z

** expression

$$\frac{\sqrt{30}Q_vxy}{5} - \frac{\sqrt{30}Q_{xy}(x-y)(x+y)}{10} + \frac{\sqrt{30}Q_{xzyz}}{10} - \frac{\sqrt{30}Q_{yzzx}}{10}$$

$$\vec{G}_1^{(2,1)}[q](B_1)$$

** symmetry

y

** expression

$$\frac{3\sqrt{10}Q_{uxz}}{10} - \frac{\sqrt{30}Q_{vzx}}{10} - \frac{\sqrt{30}Q_{xyyz}}{10} + \frac{\sqrt{30}Q_{xz}(x-z)(x+z)}{10} + \frac{\sqrt{30}Q_{yzyx}}{10}$$

$$\vec{G}_1^{(2,1)}[q](B_2)$$

** symmetry

x

** expression

$$-\frac{3\sqrt{10}Q_{uyz}}{10} - \frac{\sqrt{30}Q_{vyz}}{10} + \frac{\sqrt{30}Q_{xyxz}}{10} - \frac{\sqrt{30}Q_{xzyx}}{10} - \frac{\sqrt{30}Q_{yz}(y-z)(y+z)}{10}$$

* Harmonics for rank 2

$$\vec{G}_2^{(2,-1)}[q](A_1)$$

** symmetry

$$\sqrt{3}xy$$

** expression

$$-\frac{\sqrt{6}Q_vz}{3} + \frac{\sqrt{6}Q_{xzx}}{6} - \frac{\sqrt{6}Q_{yzy}}{6}$$

$$\vec{G}_2^{(2,1)}[q](A_1)$$

** symmetry

$$\sqrt{3}xy$$

** expression

$$\frac{5\sqrt{42}Q_{uz}(x-y)(x+y)}{28} - \frac{\sqrt{14}Q_{vz}(3x^2+3y^2-2z^2)}{28} + \frac{\sqrt{14}Q_{xzx}(2x^2-3y^2-3z^2)}{14} + \frac{\sqrt{14}Q_{yzy}(3x^2-2y^2+3z^2)}{14}$$

$$\vec{G}_2^{(2,-1)}[q](A_2, 1)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{\sqrt{2}Q_{xzy}}{2} - \frac{\sqrt{2}Q_{yzyx}}{2}$$

$$\vec{G}_2^{(2,-1)}[q](A_2, 2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{6}Q_{xyx}}{3} - \frac{\sqrt{6}Q_{xzy}}{6} - \frac{\sqrt{6}Q_{yzyx}}{6}$$

$$\vec{G}_2^{(2,1)}[q](A_2, 1)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{5\sqrt{42}Q_vxyz}{14} - \frac{5\sqrt{42}Q_{xyz}(x-y)(x+y)}{28} - \frac{\sqrt{42}Q_{xzy}(x^2+y^2-4z^2)}{28} + \frac{\sqrt{42}Q_{yzx}(x^2+y^2-4z^2)}{28}$$

$$\vec{\mathbb{G}}_2^{(2,1)}[q](A_2, 2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

** expression

$$-\frac{5\sqrt{42}Q_{uxyz}}{14} + \frac{\sqrt{14}Q_{xyz}(3x^2+3y^2-2z^2)}{28} - \frac{\sqrt{14}Q_{xzy}(9x^2-y^2-6z^2)}{28} + \frac{\sqrt{14}Q_{yzx}(x^2-9y^2+6z^2)}{28}$$

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](B_1)$$

** symmetry

$$\sqrt{3}yz$$

** expression

$$\frac{\sqrt{2}Q_{ux}}{2} + \frac{\sqrt{6}Q_{vx}}{6} + \frac{\sqrt{6}Q_{xyy}}{6} - \frac{\sqrt{6}Q_{xzz}}{6}$$

$$\vec{\mathbb{G}}_2^{(2,1)}[q](B_1)$$

** symmetry

$$\sqrt{3}yz$$

** expression

$$-\frac{\sqrt{42}Q_{ux}(x^2+y^2-4z^2)}{28} - \frac{\sqrt{14}Q_{vx}(x^2-9y^2+6z^2)}{28} - \frac{\sqrt{14}Q_{xyy}(3x^2-2y^2+3z^2)}{14} + \frac{\sqrt{14}Q_{xzz}(3x^2+3y^2-2z^2)}{14}$$

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](B_2)$$

** symmetry

$$\sqrt{3}xz$$

** expression

$$-\frac{\sqrt{2}Q_{uy}}{2} + \frac{\sqrt{6}Q_{vy}}{6} - \frac{\sqrt{6}Q_{xyx}}{6} + \frac{\sqrt{6}Q_{yzz}}{6}$$

$$\vec{\mathbb{G}}_2^{(2,1)}[q](B_2)$$

** symmetry

$$\sqrt{3}xz$$

** expression

$$\frac{\sqrt{42}Q_{uy}(x^2+y^2-4z^2)}{28} + \frac{\sqrt{14}Q_{vy}(9x^2-y^2-6z^2)}{28} - \frac{\sqrt{14}Q_{xyx}(2x^2-3y^2-3z^2)}{14} - \frac{\sqrt{14}Q_{yzz}(3x^2+3y^2-2z^2)}{14}$$

* Harmonics for rank 3

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](A_1)$$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$\frac{\sqrt{6}Q_u(x-y)(x+y)}{4} + \frac{\sqrt{2}Q_v(x^2+y^2-2z^2)}{4}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](A_1)$$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$-\frac{\sqrt{3}Q_u(x-y)(x+y)(x^2+y^2-6z^2)}{6} - \frac{Q_v(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4)}{6} - \frac{7Q_{xyxy}(x-y)(x+y)}{6} + \frac{7Q_{xzxz}(x-z)(x+z)}{6} - \frac{7Q_{yzyz}(y-z)(y+z)}{6}$$

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](A_2, 1)$$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{30}Q_vxy}{10} + \frac{\sqrt{30}Q_{xy}(x-y)(x+y)}{20} + \frac{\sqrt{30}Q_{xzyz}}{5} - \frac{\sqrt{30}Q_{yzxz}}{5}$$

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](A_2, 2)$$

** symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{6}Q_vxy}{2} - \frac{\sqrt{2}Q_{xy}(x^2 + y^2 - 2z^2)}{4}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](A_2, 1)$$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{15}Q_vxy(x^2 + y^2 - 6z^2)}{6} + \frac{\sqrt{15}Q_{xy}(x-y)(x+y)(x^2 + y^2 - 6z^2)}{12} - \frac{\sqrt{15}Q_{xzyz}(3x^2 + 3y^2 - 4z^2)}{12} + \frac{\sqrt{15}Q_{yzxz}(3x^2 + 3y^2 - 4z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](A_2, 2)$$

** symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{3}Q_vxy(x^2 + y^2 - 6z^2)}{3} + \frac{7Q_vxy(x-y)(x+y)}{6} - \frac{Q_{xy}(5x^4 - 18x^2y^2 - 12x^2z^2 + 5y^4 - 12y^2z^2 + 4z^4)}{12} - \frac{7Q_{xzyz}(3x^2 + y^2 - 2z^2)}{12} - \frac{7Q_{yzxz}(x^2 + 3y^2 - 2z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](B_1, 1)$$

** symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

** expression

$$-\frac{3\sqrt{10}Q_vxz}{20} + \frac{\sqrt{30}Q_vxz}{20} - \frac{\sqrt{30}Q_{xyyz}}{5} - \frac{\sqrt{30}Q_{xz}(x-z)(x+z)}{20} + \frac{\sqrt{30}Q_{yzxy}}{5}$$

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](B_1, 2)$$

** symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

** expression

$$\frac{\sqrt{6}Q_vxz}{4} + \frac{3\sqrt{2}Q_vxz}{4} - \frac{\sqrt{2}Q_{xz}(x^2 - 2y^2 + z^2)}{4}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](B_1, 1)$$

** symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

** expression

$$-\frac{\sqrt{5}Q_vxz(x^2 - 6y^2 + z^2)}{4} + \frac{\sqrt{15}Q_vxz(x^2 - 6y^2 + z^2)}{12} + \frac{\sqrt{15}Q_{xyyz}(3x^2 - 4y^2 + 3z^2)}{12} - \frac{\sqrt{15}Q_{xz}(x-z)(x+z)(x^2 - 6y^2 + z^2)}{12} - \frac{\sqrt{15}Q_{yzxy}(3x^2 - 4y^2 + 3z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](B_1, 2)$$

** symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

** expression

$$-\frac{\sqrt{3}Q_u xz(9x^2 - 12y^2 - 5z^2)}{12} + \frac{Q_v xz(x^2 + 36y^2 - 13z^2)}{12} - \frac{7Q_{xy} yz(3x^2 - 2y^2 + z^2)}{12} - \frac{Q_{xz}(5x^4 - 12x^2y^2 - 18x^2z^2 + 4y^4 - 12y^2z^2 + 5z^4)}{12} - \frac{7Q_{yz} xy(x^2 - 2y^2 + 3z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](B_2, 1)$$

** symmetry

$$\frac{x(2x^2 - 3y^2 - 3z^2)}{2}$$

** expression

$$\frac{3\sqrt{10}Q_u yz}{20} + \frac{\sqrt{30}Q_v yz}{20} + \frac{\sqrt{30}Q_{xy} xz}{5} - \frac{\sqrt{30}Q_{xz} xy}{5} + \frac{\sqrt{30}Q_{yz}(y-z)(y+z)}{20}$$

$$\vec{\mathbb{G}}_3^{(2,-1)}[q](B_2, 2)$$

** symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

** expression

$$\frac{\sqrt{6}Q_u yz}{4} - \frac{3\sqrt{2}Q_v yz}{4} + \frac{\sqrt{2}Q_{yz}(2x^2 - y^2 - z^2)}{4}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](B_2, 1)$$

** symmetry

$$\frac{x(2x^2 - 3y^2 - 3z^2)}{2}$$

** expression

$$-\frac{\sqrt{5}Q_u yz(6x^2 - y^2 - z^2)}{4} - \frac{\sqrt{15}Q_v yz(6x^2 - y^2 - z^2)}{12} + \frac{\sqrt{15}Q_{xy} xz(4x^2 - 3y^2 - 3z^2)}{12} - \frac{\sqrt{15}Q_{xz} xy(4x^2 - 3y^2 - 3z^2)}{12} - \frac{\sqrt{15}Q_{yz}(y-z)(y+z)(6x^2 - y^2 - z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(2,1)}[q](B_2, 2)$$

** symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

** expression

$$\frac{\sqrt{3}Q_u yz(12x^2 - 9y^2 + 5z^2)}{12} - \frac{Q_v yz(36x^2 + y^2 - 13z^2)}{12} + \frac{7Q_{xy} xz(2x^2 - 3y^2 - z^2)}{12} + \frac{7Q_{xz} xy(2x^2 - y^2 - 3z^2)}{12} - \frac{Q_{yz}(4x^4 - 12x^2y^2 - 12x^2z^2 + 5y^4 - 18y^2z^2 + 5z^4)}{12}$$

* Harmonics for rank 4

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](A_1, 1)$$

** symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{3}Q_v z(x-y)(x+y)}{2} + \sqrt{3}Q_{xy} xyz + \frac{\sqrt{3}Q_{xz} x(x^2 - 3y^2)}{4} - \frac{\sqrt{3}Q_{yz} y(3x^2 - y^2)}{4}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](A_1, 2)$$

** symmetry

$$-\frac{\sqrt{5}xy(x^2 + y^2 - 6z^2)}{2}$$

** expression

$$\frac{3\sqrt{7}Q_u z(x-y)(x+y)}{7} + \frac{\sqrt{21}Q_v z(3x^2 + 3y^2 - 2z^2)}{14} - \frac{\sqrt{21}Q_{xz} x(x^2 - 5y^2 + 2z^2)}{28} - \frac{\sqrt{21}Q_{yz} y(5x^2 - y^2 - 2z^2)}{28}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](A_1, 1)$$

** symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

** expression

$$\frac{9\sqrt{154}Q_u z (x^2 - 2xy - y^2) (x^2 + 2xy - y^2)}{88} - \frac{\sqrt{462}Q_v z (x-y)(x+y)(x^2 + y^2 - 2z^2)}{88} + \frac{\sqrt{462}Q_{xy}xyz (x^2 + y^2 - 2z^2)}{44} + \frac{\sqrt{462}Q_{xz}x (x^4 - 8x^2y^2 - 2x^2z^2 + 3y^4 + 6y^2z^2)}{44} + \frac{\sqrt{462}Q_{yz}y (3x^4 - 8x^2y^2 + 6x^2z^2 + y^4 - 2y^2z^2)}{44}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](A_1, 2)$$

** symmetry

$$-\frac{\sqrt{5}xy(x^2 + y^2 - 6z^2)}{2}$$

** expression

$$-\frac{21\sqrt{22}Q_u z (x-y)(x+y)(x^2 + y^2 - 2z^2)}{88} - \frac{\sqrt{66}Q_v z (3x^4 - 78x^2y^2 + 20x^2z^2 + 3y^4 + 20y^2z^2 - 4z^4)}{88} - \frac{21\sqrt{66}Q_{xy}xyz (x-y)(x+y)}{44} - \frac{\sqrt{66}Q_{xz}x (x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{44} + \frac{\sqrt{66}Q_{yz}y (x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{44}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](A_2, 1)$$

** symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

** expression

$$\frac{\sqrt{5}Q_{xyz}(x-y)(x+y)}{2} - \frac{\sqrt{5}Q_{xz}y(x-z)(x+z)}{2} + \frac{\sqrt{5}Q_{yz}x(y-z)(y+z)}{2}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](A_2, 2)$$

** symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

** expression

$$-\frac{6\sqrt{7}Q_vxyz}{7} - \frac{\sqrt{7}Q_{xyz}(x-y)(x+y)}{14} + \frac{\sqrt{7}Q_{xz}y(4x^2 - 3y^2 + 5z^2)}{14} + \frac{\sqrt{7}Q_{yz}x(3x^2 - 4y^2 - 5z^2)}{14}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](A_2, 3)$$

** symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2 + y^2 - 6z^2)}{4}$$

** expression

$$\frac{6\sqrt{7}Q_uxyz}{7} + \frac{\sqrt{21}Q_{xyz}(3x^2 + 3y^2 - 2z^2)}{14} - \frac{\sqrt{21}Q_{xz}y(2x^2 - y^2 + z^2)}{14} + \frac{\sqrt{21}Q_{yz}x(x^2 - 2y^2 - z^2)}{14}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](A_2, 1)$$

** symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

** expression

$$-\frac{3\sqrt{2310}Q_uxyz(x-y)(x+y)}{44} - \frac{3\sqrt{770}Q_vxyz(x^2 + y^2 - 2z^2)}{44} + \frac{\sqrt{770}Q_{xyz}(x-y)(x+y)(x^2 + y^2 - 2z^2)}{22} - \frac{\sqrt{770}Q_{xz}y(x-z)(x+z)(x^2 - 2y^2 + z^2)}{22} - \frac{\sqrt{770}Q_{yz}x(y-z)(y+z)(2x^2 - y^2 - z^2)}{22}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](A_2, 2)$$

** symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

** expression

$$\frac{21\sqrt{66}Q_uxyz(x-y)(x+y)}{44} - \frac{21\sqrt{22}Q_vxyz(x^2+y^2-2z^2)}{44} + \frac{7\sqrt{22}Q_{xy}z(x-y)(x+y)(x^2+y^2-2z^2)}{44} + \frac{\sqrt{22}Q_{xz}y(17x^4-22x^2y^2-36x^2z^2+3y^4-8y^2z^2+10z^4)}{44} - \frac{\sqrt{22}Q_{yz}x(3x^4-22x^2y^2-8x^2z^2+17y^4-36y^2z^2+10z^4)}{44}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](A_2, 3)$$

** symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

** expression

$$-\frac{21\sqrt{22}Q_uxyz(x^2+y^2-2z^2)}{44} - \frac{21\sqrt{66}Q_vxyz(x-y)(x+y)}{44} + \frac{\sqrt{66}Q_{xy}z(9x^4-24x^2y^2-10x^2z^2+9y^4-10y^2z^2+2z^4)}{44} - \frac{\sqrt{66}Q_{xz}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44} - \frac{\sqrt{66}Q_{yz}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](B_1, 1)$$

** symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

** expression

$$\frac{3Q_u x(y-z)(y+z)}{4} + \frac{\sqrt{3}Q_v x(y-z)(y+z)}{4} + \frac{\sqrt{3}Q_{xy}y(y^2-3z^2)}{4} - \frac{\sqrt{3}Q_{xz}z(3y^2-z^2)}{4} + \sqrt{3}Q_{yz}xyz$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](B_1, 2)$$

** symmetry

$$\frac{\sqrt{5}yz(6x^2-y^2-z^2)}{2}$$

** expression

$$\frac{3\sqrt{7}Q_u x(2x^2-5y^2-z^2)}{28} + \frac{\sqrt{21}Q_v x(2x^2+3y^2-9z^2)}{28} - \frac{\sqrt{21}Q_{xy}y(2x^2+y^2-5z^2)}{28} + \frac{\sqrt{21}Q_{xz}z(2x^2-5y^2+z^2)}{28}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](B_1, 1)$$

** symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

** expression

$$-\frac{3\sqrt{154}Q_u x(x^2y^2-x^2z^2+y^4-9y^2z^2+2z^4)}{88} - \frac{\sqrt{462}Q_v x(x^2y^2-x^2z^2-5y^4+27y^2z^2-4z^4)}{88} - \frac{\sqrt{462}Q_{xy}y(2x^2y^2-6x^2z^2-y^4+8y^2z^2-3z^4)}{44} + \frac{\sqrt{462}Q_{xz}z(6x^2y^2-2x^2z^2+3y^4-8y^2z^2+z^4)}{44} - \frac{\sqrt{462}Q_{yz}xyz(2x^2-y^2-z^2)}{44}$$

$$\vec{\mathbb{G}}_4^{(2,1)}[q](B_1, 2)$$

** symmetry

$$\frac{\sqrt{5}yz(6x^2-y^2-z^2)}{2}$$

** expression

$$-\frac{3\sqrt{22}Q_u x(2x^4-3x^2y^2-17x^2z^2-5y^4+39y^2z^2+2z^4)}{88} - \frac{\sqrt{66}Q_v x(2x^4-31x^2y^2+11x^2z^2+9y^4+39y^2z^2-12z^4)}{88} - \frac{\sqrt{66}Q_{xy}y(8x^4-12x^2y^2-12x^2z^2+y^4+2y^2z^2+z^4)}{44} + \frac{\sqrt{66}Q_{xz}z(8x^4-12x^2y^2-12x^2z^2+y^4+2y^2z^2+z^4)}{44} - \frac{21\sqrt{66}Q_{yz}xyz(y-z)(y+z)}{44}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](B_2, 1)$$

** symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

** expression

$$\frac{3Q_u y(x-z)(x+z)}{4} - \frac{\sqrt{3}Q_v y(x-z)(x+z)}{4} + \frac{\sqrt{3}Q_{xy}x(x^2-3z^2)}{4} + \sqrt{3}Q_{xz}xyz - \frac{\sqrt{3}Q_{yz}z(3x^2-z^2)}{4}$$

$$\vec{\mathbb{G}}_4^{(2,-1)}[q](B_2, 2)$$

** symmetry

$$-\frac{\sqrt{5}xz(x^2 - 6y^2 + z^2)}{2}$$

** expression

$$\frac{3\sqrt{7}Q_{uy}(5x^2 - 2y^2 + z^2)}{28} + \frac{\sqrt{21}Q_{vy}(3x^2 + 2y^2 - 9z^2)}{28} + \frac{\sqrt{21}Q_{xyx}(x^2 + 2y^2 - 5z^2)}{28} + \frac{\sqrt{21}Q_{yzz}(5x^2 - 2y^2 - z^2)}{28}$$

$\vec{\mathbb{G}}_4^{(2,1)}[q](B_2, 1)$

** symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

** expression

$$\begin{aligned} &-\frac{3\sqrt{154}Q_{uy}(x^4 + x^2y^2 - 9x^2z^2 - y^2z^2 + 2z^4)}{88} - \frac{\sqrt{462}Q_{vy}(5x^4 - x^2y^2 - 27x^2z^2 + y^2z^2 + 4z^4)}{88} \\ &+ \frac{\sqrt{462}Q_{xyx}(x^4 - 2x^2y^2 - 8x^2z^2 + 6y^2z^2 + 3z^4)}{44} + \frac{\sqrt{462}Q_{xzx}xyz(x^2 - 2y^2 + z^2)}{44} + \frac{\sqrt{462}Q_{yzz}(3x^4 + 6x^2y^2 - 8x^2z^2 - 2y^2z^2 + z^4)}{44} \end{aligned}$$

$\vec{\mathbb{G}}_4^{(2,1)}[q](B_2, 2)$

** symmetry

$$-\frac{\sqrt{5}xz(x^2 - 6y^2 + z^2)}{2}$$

** expression

$$\begin{aligned} &-\frac{3\sqrt{22}Q_{uy}(5x^4 + 3x^2y^2 - 39x^2z^2 - 2y^4 + 17y^2z^2 - 2z^4)}{88} - \frac{\sqrt{66}Q_{vy}(9x^4 - 31x^2y^2 + 39x^2z^2 + 2y^4 + 11y^2z^2 - 12z^4)}{88} \\ &+ \frac{\sqrt{66}Q_{xyx}(x^4 - 12x^2y^2 + 2x^2z^2 + 8y^4 - 12y^2z^2 + z^4)}{44} + \frac{21\sqrt{66}Q_{xzx}xyz(x-z)(x+z)}{44} - \frac{\sqrt{66}Q_{yzz}(x^4 - 12x^2y^2 + 2x^2z^2 + 8y^4 - 12y^2z^2 + z^4)}{44} \end{aligned}$$