

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag                | matrix (polar)   | det | TR |
|-----|--------------------|--|-----|----|
| 1   | $\{1 0\}$          | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$    | 1   | 1  |
| 2   | $\{2_{001} 0\}$    | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$  | 1   | 1  |
| 3   | $\{2_{110} 0\}$    | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$   | 1   | 1  |
| 4   | $\{2_{1-10} 0\}$   | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | 1   | 1  |
| 5   | $\{-4_{001}^+ 0\}$ | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$  | -1  | -1 |
| 6   | $\{-4_{001}^- 0\}$ | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$  | -1  | -1 |
| 7   | $\{m_{100}' 0\}$   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$   | -1  | -1 |
| 8   | $\{m_{010}' 0\}$   | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$   | -1  | -1 |