PG No. 5 $C_{2\mathrm{h}}$ $2/m$ (b-axis setting) [monoclinic] (polar, internal axial dipole)

* Harmonics for rank 0
* Harmonics for rank 1

$\vec{\mathbb{Q}}_1^{(1,0)}[g](A_u)$

** symmetry

$$y$$

** expression

$$-\frac{\sqrt{2}G_x z}{2}+\frac{\sqrt{2}G_z x}{2}$$

$\vec{\mathbb{Q}}_1^{(1,0)}[g](B_u,1)$

** symmetry

$$x$$

** expression

$$\frac{\sqrt{2}G_y z}{2}-\frac{\sqrt{2}G_z y}{2}$$

$\vec{\mathbb{Q}}_1^{(1,0)}[g](B_u,2)$

** symmetry

$$z$$

** expression

$$\frac{\sqrt{2}G_x y}{2}-\frac{\sqrt{2}G_y x}{2}$$

* Harmonics for rank 2

$\vec{\mathbb{Q}}_2^{(1,0)}[g](A_g,1)$

** symmetry

$$-\frac{x^2}{2}-\frac{y^2}{2}+z^2$$

** expression

$$\frac{\sqrt{6}G_x yz}{2}-\frac{\sqrt{6}G_y xz}{2}$$

$\vec{\mathbb{Q}}_2^{(1,0)}[g](A_g,2)$

** symmetry

$$\frac{\sqrt{3}\,(x-y)\,(x+y)}{2}$$

** expression

$$\frac{\sqrt{2}G_x yz}{2}+\frac{\sqrt{2}G_y xz}{2}-\sqrt{2}G_z xy$$

$\vec{\mathbb{Q}}_2^{(1,0)}[g](A_g,3)$

** symmetry

$$\sqrt{3}xz$$

** expression

$$\frac{\sqrt{2}G_x xy}{2}-\frac{\sqrt{2}G_y\,(x-z)\,(x+z)}{2}-\frac{\sqrt{2}G_z yz}{2}$$

$\vec{\mathbb{Q}}_2^{(1,0)}[g](B_g,1)$

** symmetry

$$\sqrt{3}yz$$

** expression

$$\frac{\sqrt{2}G_x\,(y-z)\,(y+z)}{2}-\frac{\sqrt{2}G_y xy}{2}+\frac{\sqrt{2}G_z xz}{2}$$

$\vec{\mathbb{Q}}_2^{(1,0)}[g](B_g,2)$

** symmetry

$$\sqrt{3}xy$$

** expression

$$-\frac{\sqrt{2}G_x xz}{2}+\frac{\sqrt{2}G_y yz}{2}+\frac{\sqrt{2}G_z\left(x-y\right)\left(x+y\right)}{2}$$

* Harmonics for rank 3

$\vec{\mathbb{Q}}_3^{(1,0)}[g](A_u,1)$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$\frac{\sqrt{5}G_x x\left(y-z\right)\left(y+z\right)}{2}-\frac{\sqrt{5}G_y y\left(x-z\right)\left(x+z\right)}{2}+\frac{\sqrt{5}G_z z\left(x-y\right)\left(x+y\right)}{2}$$

$\vec{\mathbb{Q}}_3^{(1,0)}[g](A_u,2)$

** symmetry

$$-\frac{y\left(3x^2-2y^2+3z^2\right)}{2}$$

** expression

$$\frac{\sqrt{3}G_x z\left(x^2-4y^2+z^2\right)}{4}-\frac{\sqrt{3}G_z x\left(x^2-4y^2+z^2\right)}{4}$$

$\vec{\mathbb{Q}}_3^{(1,0)}[g](A_u,3)$

** symmetry

$$-\frac{\sqrt{15}y\left(x-z\right)\left(x+z\right)}{2}$$

** expression

$$\frac{\sqrt{5}G_x z\left(x^2+2y^2-z^2\right)}{4}-\sqrt{5}G_y xyz-\frac{\sqrt{5}G_z x\left(x^2-2y^2-z^2\right)}{4}$$

$\vec{\mathbb{Q}}_3^{(1,0)}[g](B_u,1)$

** symmetry

$$\frac{x\left(2x^2-3y^2-3z^2\right)}{2}$$

** expression

$$\frac{\sqrt{3}G_y z\left(4x^2-y^2-z^2\right)}{4}-\frac{\sqrt{3}G_z y\left(4x^2-y^2-z^2\right)}{4}$$

$\vec{\mathbb{Q}}_3^{(1,0)}[g](B_u,2)$

** symmetry

$$-\frac{z\left(3x^2+3y^2-2z^2\right)}{2}$$

** expression

$$-\frac{\sqrt{3}G_x y\left(x^2+y^2-4z^2\right)}{4}+\frac{\sqrt{3}G_y x\left(x^2+y^2-4z^2\right)}{4}$$

$\vec{\mathbb{Q}}_3^{(1,0)}[g](B_u,3)$

** symmetry

$$\frac{\sqrt{15}x\left(y-z\right)\left(y+z\right)}{2}$$

** expression

$$-\sqrt{5}G_x xyz+\frac{\sqrt{5}G_y z\left(2x^2+y^2-z^2\right)}{4}+\frac{\sqrt{5}G_z y\left(2x^2-y^2+z^2\right)}{4}$$

$\vec{\mathbb{Q}}_3^{(1,0)}[g](B_u,4)$

** symmetry

$$\frac{\sqrt{15}z\left(x-y\right)\left(x+y\right)}{2}$$

** expression

$$\frac{\sqrt{5}G_x y\left(x^2-y^2+2z^2\right)}{4}-\frac{\sqrt{5}G_y x\left(x^2-y^2-2z^2\right)}{4}-\sqrt{5}G_z xyz$$

* Harmonics for rank 4

$\vec{\mathbb{Q}}_4^{(1,0)}[g](A_g,1)$

** symmetry

$$\frac{\sqrt{21}\left(x^4-3x^2y^2-3x^2z^2+y^4-3y^2z^2+z^4\right)}{6}$$

** expression

$$-\frac{\sqrt{105}G_xyz\,(y-z)\,(y+z)}{6}+\frac{\sqrt{105}G_yxz\,(x-z)\,(x+z)}{6}-\frac{\sqrt{105}G_zxy\,(x-y)\,(x+y)}{6}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](A_g,2)$

** symmetry

$$-\frac{\sqrt{15}\left(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4\right)}{12}$$

** expression

$$-\frac{\sqrt{3}G_xyz\left(9x^2+2y^2-5z^2\right)}{6}+\frac{\sqrt{3}G_yxz\left(2x^2+9y^2-5z^2\right)}{6}+\frac{7\sqrt{3}G_zxy\,(x-y)\,(x+y)}{6}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](A_g,3)$

** symmetry

$$\frac{\sqrt{5}\,(x-y)\,(x+y)\left(x^2+y^2-6z^2\right)}{4}$$

** expression

$$-\frac{G_xyz\left(3x^2-4y^2+3z^2\right)}{2}+\frac{G_yxz\left(4x^2-3y^2-3z^2\right)}{2}-\frac{G_zxy\left(x^2+y^2-6z^2\right)}{2}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](A_g,4)$

** symmetry

$$-\frac{\sqrt{35}xz\,(x-z)\,(x+z)}{2}$$

** expression

$$-\frac{\sqrt{7}G_xxy\left(x^2-3z^2\right)}{4}+\frac{\sqrt{7}G_y\left(x^2-2xz-z^2\right)\left(x^2+2xz-z^2\right)}{4}+\frac{\sqrt{7}G_zyz\left(3x^2-z^2\right)}{4}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](A_g,5)$

** symmetry

$$-\frac{\sqrt{5}xz\left(x^2-6y^2+z^2\right)}{2}$$

** expression

$$-\frac{G_xxy\left(x^2-6y^2+15z^2\right)}{4}+\frac{G_y\,(x-z)\,(x+z)\left(x^2-6y^2+z^2\right)}{4}+\frac{G_zyz\left(15x^2-6y^2+z^2\right)}{4}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](B_g,1)$

** symmetry

$$\frac{\sqrt{35}yz\,(y-z)\,(y+z)}{2}$$

** expression

$$\frac{\sqrt{7}G_x\left(y^2-2yz-z^2\right)\left(y^2+2yz-z^2\right)}{4}-\frac{\sqrt{7}G_yxy\left(y^2-3z^2\right)}{4}+\frac{\sqrt{7}G_zxz\left(3y^2-z^2\right)}{4}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](B_g,2)$

** symmetry

$$\frac{\sqrt{35}xy\,(x-y)\,(x+y)}{2}$$

** expression

$$-\frac{\sqrt{7}G_xxz\left(x^2-3y^2\right)}{4}+\frac{\sqrt{7}G_yyz\left(3x^2-y^2\right)}{4}+\frac{\sqrt{7}G_z\left(x^2-2xy-y^2\right)\left(x^2+2xy-y^2\right)}{4}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](B_g,3)$

** symmetry

$$\frac{\sqrt{5}yz\left(6x^2-y^2-z^2\right)}{2}$$

** expression

$$\frac{G_x\left(y-z\right)\left(y+z\right)\left(6x^2-y^2-z^2\right)}{4}-\frac{G_yxy\left(6x^2-y^2-15z^2\right)}{4}+\frac{G_zxz\left(6x^2-15y^2-z^2\right)}{4}$$

$\vec{\mathbb{Q}}_4^{(1,0)}[g](B_g,4)$
** symmetry

$$-\frac{\sqrt{5}xy\left(x^2+y^2-6z^2\right)}{2}$$

** expression

$$\frac{G_xxz\left(x^2+15y^2-6z^2\right)}{4}-\frac{G_yyz\left(15x^2+y^2-6z^2\right)}{4}-\frac{G_z\left(x-y\right)\left(x+y\right)\left(x^2+y^2-6z^2\right)}{4}$$