

PG No. 21 C_6 6 [hexagonal] (polar, internal axial quadrupole)

* Harmonics for rank 0

* Harmonics for rank 1

$$\bar{Q}_1^{(2,1)}[g](A)$$

** symmetry

$$z$$

** expression

$$\frac{\sqrt{30}G_vxy}{5} - \frac{\sqrt{30}G_{xy}(x-y)(x+y)}{10} + \frac{\sqrt{30}G_{xz}yz}{10} - \frac{\sqrt{30}G_{yz}xz}{10}$$

$$\bar{Q}_{1,1}^{(2,1)}[g](E_1), \bar{Q}_{1,2}^{(2,1)}[g](E_1)$$

** symmetry

$$x$$

$$y$$

** expression

$$-\frac{3\sqrt{10}G_uyz}{10} - \frac{\sqrt{30}G_vyz}{10} + \frac{\sqrt{30}G_{xy}xz}{10} - \frac{\sqrt{30}G_{xz}xy}{10} - \frac{\sqrt{30}G_{yz}(y-z)(y+z)}{10}$$

$$\frac{3\sqrt{10}G_uxz}{10} - \frac{\sqrt{30}G_vxz}{10} - \frac{\sqrt{30}G_{xy}yz}{10} + \frac{\sqrt{30}G_{xz}(x-z)(x+z)}{10} + \frac{\sqrt{30}G_{yz}xy}{10}$$

* Harmonics for rank 2

$$\bar{Q}_2^{(2,-1)}[g](A)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{\sqrt{2}G_{xz}y}{2} - \frac{\sqrt{2}G_{yz}x}{2}$$

$$\bar{Q}_2^{(2,1)}[g](A)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{5\sqrt{42}G_vxyz}{14} - \frac{5\sqrt{42}G_{xyz}(x-y)(x+y)}{28} - \frac{\sqrt{42}G_{xz}y(x^2+y^2-4z^2)}{28} + \frac{\sqrt{42}G_{yz}x(x^2+y^2-4z^2)}{28}$$

$$\bar{Q}_{2,1}^{(2,-1)}[g](E_1), \bar{Q}_{2,2}^{(2,-1)}[g](E_1)$$

** symmetry

$$\sqrt{3}yz$$

$$-\sqrt{3}xz$$

** expression

$$\frac{\sqrt{2}G_ux}{2} + \frac{\sqrt{6}G_vx}{6} + \frac{\sqrt{6}G_{xy}y}{6} - \frac{\sqrt{6}G_{xz}z}{6}$$

$$\frac{\sqrt{2}G_uy}{2} - \frac{\sqrt{6}G_vy}{6} + \frac{\sqrt{6}G_{xy}x}{6} - \frac{\sqrt{6}G_{yz}z}{6}$$

$$\bar{Q}_{2,1}^{(2,1)}[g](E_1), \bar{Q}_{2,2}^{(2,1)}[g](E_1)$$

** symmetry

$$\sqrt{3}yz$$

$$-\sqrt{3}xz$$

** expression

$$-\frac{\sqrt{42}G_ux(x^2+y^2-4z^2)}{28} - \frac{\sqrt{14}G_vx(x^2-9y^2+6z^2)}{28} - \frac{\sqrt{14}G_{xy}y(3x^2-2y^2+3z^2)}{14} + \frac{\sqrt{14}G_{xz}z(3x^2+3y^2-2z^2)}{14}$$

$$-\frac{\sqrt{42}G_u y (x^2 + y^2 - 4z^2)}{28} - \frac{\sqrt{14}G_v y (9x^2 - y^2 - 6z^2)}{28} + \frac{\sqrt{14}G_{xy} x (2x^2 - 3y^2 - 3z^2)}{14} + \frac{\sqrt{14}G_{yz} z (3x^2 + 3y^2 - 2z^2)}{14}$$

$$\bar{Q}_{2,1}^{(2,-1)}[g](E_2), \bar{Q}_{2,2}^{(2,-1)}[g](E_2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

$$-\sqrt{3}xy$$

** expression

$$\frac{\sqrt{6}G_{xyz}}{3} - \frac{\sqrt{6}G_{xzy}}{6} - \frac{\sqrt{6}G_{yzx}}{6}$$

$$\frac{\sqrt{6}G_v z}{3} - \frac{\sqrt{6}G_{zx} x}{6} + \frac{\sqrt{6}G_{yz} y}{6}$$

$$\bar{Q}_{2,1}^{(2,1)}[g](E_2), \bar{Q}_{2,2}^{(2,1)}[g](E_2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

$$-\sqrt{3}xy$$

** expression

$$-\frac{5\sqrt{42}G_u xyz}{14} + \frac{\sqrt{14}G_{xy} z (3x^2 + 3y^2 - 2z^2)}{28} - \frac{\sqrt{14}G_{xzy} (9x^2 - y^2 - 6z^2)}{28} + \frac{\sqrt{14}G_{yz} x (x^2 - 9y^2 + 6z^2)}{28}$$

$$-\frac{5\sqrt{42}G_u z (x-y)(x+y)}{28} + \frac{\sqrt{14}G_v z (3x^2 + 3y^2 - 2z^2)}{28} - \frac{\sqrt{14}G_{zx} x (2x^2 - 3y^2 - 3z^2)}{14} - \frac{\sqrt{14}G_{yz} y (3x^2 - 2y^2 + 3z^2)}{14}$$

* Harmonics for rank 3

$$\bar{Q}_3^{(2,-1)}[g](A)$$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{30}G_v xy}{10} + \frac{\sqrt{30}G_{xy} (x-y)(x+y)}{20} + \frac{\sqrt{30}G_{xzy} z}{5} - \frac{\sqrt{30}G_{yz} xz}{5}$$

$$\bar{Q}_3^{(2,1)}[g](A)$$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{15}G_v xy (x^2 + y^2 - 6z^2)}{6} + \frac{\sqrt{15}G_{xy} (x-y)(x+y)(x^2 + y^2 - 6z^2)}{12} - \frac{\sqrt{15}G_{xzy} z (3x^2 + 3y^2 - 4z^2)}{12} + \frac{\sqrt{15}G_{yz} xz (3x^2 + 3y^2 - 4z^2)}{12}$$

$$\bar{Q}_3^{(2,-1)}[g](B, 1)$$

** symmetry

$$\frac{\sqrt{10}y(3x^2 - y^2)}{4}$$

** expression

$$-\frac{\sqrt{3}G_v xz}{2} + \frac{\sqrt{3}G_{xy} yz}{2} + \frac{\sqrt{3}G_{xz} (x-y)(x+y)}{4} - \frac{\sqrt{3}G_{yz} xy}{2}$$

$$\bar{Q}_3^{(2,-1)}[g](B, 2)$$

** symmetry

$$\frac{\sqrt{10}x(x^2 - 3y^2)}{4}$$

** expression

$$\frac{\sqrt{3}G_v yz}{2} + \frac{\sqrt{3}G_{xy} xz}{2} - \frac{\sqrt{3}G_{xz} xy}{2} - \frac{\sqrt{3}G_{yz} (x-y)(x+y)}{4}$$

$$\bar{Q}_3^{(2,1)}[g](B, 1)$$

** symmetry

$$\frac{\sqrt{10}y(3x^2 - y^2)}{4}$$

** expression

$$\frac{7\sqrt{2}G_u xz(x^2 - 3y^2)}{8} - \frac{\sqrt{6}G_v xz(3x^2 + 3y^2 - 4z^2)}{24} + \frac{\sqrt{6}G_{xy}yz(3x^2 + 3y^2 - 4z^2)}{24} + \frac{\sqrt{6}G_{xz}xy(11x^2 - 17y^2 + 18z^2)}{24}$$

$$\bar{Q}_3^{(2,1)}[g](B, 2)$$

** symmetry

$$\frac{\sqrt{10}x(x^2 - 3y^2)}{4}$$

** expression

$$-\frac{7\sqrt{2}G_u yz(3x^2 - y^2)}{8} + \frac{\sqrt{6}G_v yz(3x^2 + 3y^2 - 4z^2)}{24} + \frac{\sqrt{6}G_{xy}xz(3x^2 + 3y^2 - 4z^2)}{24} - \frac{\sqrt{6}G_{xz}xy(17x^2 - 11y^2 - 18z^2)}{24} + \frac{\sqrt{6}G_{yz}(2x^4 - 21x^2y^2 + 9x^2z^2 + 5y^4 - 9y^2z^2)}{24}$$

$$\bar{Q}_{3,1}^{(2,-1)}[g](E_1), \bar{Q}_{3,2}^{(2,-1)}[g](E_1)$$

** symmetry

$$-\frac{\sqrt{6}x(x^2 + y^2 - 4z^2)}{4}$$

$$-\frac{\sqrt{6}y(x^2 + y^2 - 4z^2)}{4}$$

** expression

$$-\frac{\sqrt{15}G_u yz}{5} + \frac{3\sqrt{5}G_v yz}{10} - \frac{3\sqrt{5}G_{xy}xz}{10} + \frac{3\sqrt{5}G_{xz}xy}{10} - \frac{\sqrt{5}G_{yz}(5x^2 - y^2 - 4z^2)}{20} + \frac{\sqrt{15}G_u xz}{5} + \frac{3\sqrt{5}G_v xz}{10} + \frac{3\sqrt{5}G_{xy}yz}{10} - \frac{\sqrt{5}G_{xz}(x^2 - 5y^2 + 4z^2)}{20} - \frac{3\sqrt{5}G_{yz}xy}{10}$$

$$\bar{Q}_{3,1}^{(2,1)}[g](E_1), \bar{Q}_{3,2}^{(2,1)}[g](E_1)$$

** symmetry

$$-\frac{\sqrt{6}x(x^2 + y^2 - 4z^2)}{4}$$

$$-\frac{\sqrt{6}y(x^2 + y^2 - 4z^2)}{4}$$

** expression

$$\frac{\sqrt{30}G_u yz(3x^2 + 3y^2 - 4z^2)}{24} + \frac{\sqrt{10}G_v yz(27x^2 - y^2 - 8z^2)}{24} - \frac{\sqrt{10}G_{xy}xz(13x^2 - 15y^2 - 8z^2)}{24} - \frac{\sqrt{10}G_{xz}xy(x^2 + y^2 - 6z^2)}{24} + \frac{\sqrt{10}G_{yz}(2x^4 + 3x^2y^2 - 15x^2z^2 + y^4 - 9y^2z^2 + 4z^4)}{24} - \frac{\sqrt{30}G_u xz(3x^2 + 3y^2 - 4z^2)}{24} - \frac{\sqrt{10}G_v xz(x^2 - 27y^2 + 8z^2)}{24} - \frac{\sqrt{10}G_{xy}yz(15x^2 - 13y^2 + 8z^2)}{24} - \frac{\sqrt{10}G_{xz}(x^4 + 3x^2y^2 - 9x^2z^2 + 2y^4 - 15y^2z^2 + 4z^4)}{24} + \frac{\sqrt{10}G_{yz}xy(x^2 + y^2 - 6z^2)}{24}$$

$$\bar{Q}_{3,1}^{(2,-1)}[g](E_2), \bar{Q}_{3,2}^{(2,-1)}[g](E_2)$$

** symmetry

$$\sqrt{15}xyz$$

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{6}G_u(x-y)(x+y)}{4} + \frac{\sqrt{2}G_v(x^2 + y^2 - 2z^2)}{4}$$

$$-\frac{\sqrt{6}G_u xy}{2} - \frac{\sqrt{2}G_{xy}(x^2 + y^2 - 2z^2)}{4}$$

$$\bar{Q}_{3,1}^{(2,1)}[g](E_2), \bar{Q}_{3,2}^{(2,1)}[g](E_2)$$

** symmetry

$$\sqrt{15}xyz$$

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{3}G_u(x-y)(x+y)(x^2 + y^2 - 6z^2)}{6} - \frac{G_v(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{6}$$

$$-\frac{7G_{xy}xy(x-y)(x+y)}{6} + \frac{7G_{xz}xz(x-z)(x+z)}{6} - \frac{7G_{yz}yz(y-z)(y+z)}{6}$$

$$\frac{\sqrt{3}G_u xy(x^2 + y^2 - 6z^2)}{3} + \frac{7G_v xy(x-y)(x+y)}{6} - \frac{G_{xy}(5x^4 - 18x^2y^2 - 12x^2z^2 + 5y^4 - 12y^2z^2 + 4z^4)}{12}$$

$$-\frac{7G_{xz}yz(3x^2 + y^2 - 2z^2)}{12} - \frac{7G_{yz}xz(x^2 + 3y^2 - 2z^2)}{12}$$

* Harmonics for rank 4

$$\bar{Q}_4^{(2,-1)}[g](A)$$

** symmetry

$$\frac{3x^4}{8} + \frac{3x^2y^2}{4} - 3x^2z^2 + \frac{3y^4}{8} - 3y^2z^2 + z^4$$

** expression

$$-\frac{\sqrt{105}G_vxyz}{7} + \frac{\sqrt{105}G_{xyz}(x-y)(x+y)}{14} - \frac{\sqrt{105}G_{xz}y(x^2 + y^2 - 4z^2)}{28} + \frac{\sqrt{105}G_{yz}x(x^2 + y^2 - 4z^2)}{28}$$

$$\bar{Q}_4^{(2,1)}[g](A)$$

** symmetry

$$\frac{3x^4}{8} + \frac{3x^2y^2}{4} - 3x^2z^2 + \frac{3y^4}{8} - 3y^2z^2 + z^4$$

** expression

$$-\frac{7\sqrt{330}G_vxyz(x^2 + y^2 - 2z^2)}{44} + \frac{7\sqrt{330}G_{xyz}(x-y)(x+y)(x^2 + y^2 - 2z^2)}{88}$$

$$+ \frac{\sqrt{330}G_{xz}y(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{88} - \frac{\sqrt{330}G_{yz}x(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{88}$$

$$\bar{Q}_4^{(2,-1)}[g](B, 1)$$

** symmetry

$$\frac{\sqrt{70}xz(x^2 - 3y^2)}{4}$$

** expression

$$-\frac{3\sqrt{2}G_u y(3x^2 - y^2)}{8} - \frac{\sqrt{6}G_v y(x^2 + y^2 - 4z^2)}{8} - \frac{\sqrt{6}G_{xy}x(x^2 + y^2 - 4z^2)}{8} - \frac{\sqrt{6}G_{xz}xyz}{4} - \frac{\sqrt{6}G_{yz}z(x-y)(x+y)}{8}$$

$$\bar{Q}_4^{(2,-1)}[g](B, 2)$$

** symmetry

$$\frac{\sqrt{70}yz(3x^2 - y^2)}{4}$$

** expression

$$\frac{3\sqrt{2}G_u x(x^2 - 3y^2)}{8} + \frac{\sqrt{6}G_v x(x^2 + y^2 - 4z^2)}{8} - \frac{\sqrt{6}G_{xy}y(x^2 + y^2 - 4z^2)}{8} + \frac{\sqrt{6}G_{xz}z(x-y)(x+y)}{8} - \frac{\sqrt{6}G_{yz}xyz}{4}$$

$$\bar{Q}_4^{(2,1)}[g](B, 1)$$

** symmetry

$$\frac{\sqrt{70}xz(x^2 - 3y^2)}{4}$$

** expression

$$\frac{3\sqrt{77}G_u y(3x^2 - y^2)(x^2 + y^2 - 8z^2)}{88} + \frac{\sqrt{231}G_v y(7x^4 - 16x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 4z^4)}{88}$$

$$-\frac{\sqrt{231}G_{xy}x(x^4 - 7x^2y^2 - 3x^2z^2 + 4y^4 - 3y^2z^2 + 2z^4)}{44} - \frac{\sqrt{231}G_{xz}xyz(11x^2 - y^2 - 10z^2)}{44} - \frac{\sqrt{231}G_{yz}z(x^4 + 9x^2y^2 - 5x^2z^2 - 4y^4 + 5y^2z^2)}{44}$$

$$\bar{Q}_{4,1}^{(2,1)}[g](B, 2)$$

** symmetry

$$\frac{\sqrt{70}yz(3x^2 - y^2)}{4}$$

** expression

$$\begin{aligned} & -\frac{3\sqrt{77}G_{ux}(x^2 - 3y^2)(x^2 + y^2 - 8z^2)}{88} - \frac{\sqrt{231}G_vx(x^4 - 16x^2y^2 + 6x^2z^2 + 7y^4 + 6y^2z^2 - 4z^4)}{88} \\ & - \frac{\sqrt{231}G_{xyy}(4x^4 - 7x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + 2z^4)}{44} + \frac{\sqrt{231}G_{xzz}(4x^4 - 9x^2y^2 - 5x^2z^2 - y^4 + 5y^2z^2)}{44} + \frac{\sqrt{231}G_{yzyxz}(x^2 - 11y^2 + 10z^2)}{44} \end{aligned}$$

$$\bar{Q}_{4,1}^{(2,-1)}[g](E_1), \bar{Q}_{4,2}^{(2,-1)}[g](E_1)$$

** symmetry

$$-\frac{\sqrt{10}yz(3x^2 + 3y^2 - 4z^2)}{4}$$

$$\frac{\sqrt{10}xz(3x^2 + 3y^2 - 4z^2)}{4}$$

** expression

$$\begin{aligned} & -\frac{3\sqrt{14}G_{ux}(x^2 + y^2 - 4z^2)}{56} - \frac{\sqrt{42}G_vx(x^2 + 5y^2 - 8z^2)}{56} + \frac{\sqrt{42}G_{xyy}(x^2 - 3y^2 + 8z^2)}{56} - \frac{\sqrt{42}G_{xzz}(x^2 - 13y^2 + 4z^2)}{56} - \frac{\sqrt{42}G_{yzyxz}}{4} \\ & - \frac{3\sqrt{14}G_{uy}(x^2 + y^2 - 4z^2)}{56} + \frac{\sqrt{42}G_vy(5x^2 + y^2 - 8z^2)}{56} - \frac{\sqrt{42}G_{xyx}(3x^2 - y^2 - 8z^2)}{56} - \frac{\sqrt{42}G_{xzyxz}}{4} + \frac{\sqrt{42}G_{yzz}(13x^2 - y^2 - 4z^2)}{56} \end{aligned}$$

$$\bar{Q}_{4,1}^{(2,1)}[g](E_1), \bar{Q}_{4,2}^{(2,1)}[g](E_1)$$

** symmetry

$$-\frac{\sqrt{10}yz(3x^2 + 3y^2 - 4z^2)}{4}$$

$$\frac{\sqrt{10}xz(3x^2 + 3y^2 - 4z^2)}{4}$$

** expression

$$\begin{aligned} & \frac{3\sqrt{11}G_{ux}(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{88} + \frac{\sqrt{33}G_vx(x^4 - 12x^2y^2 + 2x^2z^2 - 13y^4 + 114y^2z^2 - 20z^4)}{88} \\ & + \frac{\sqrt{33}G_{xyy}(4x^4 + x^2y^2 - 27x^2z^2 - 3y^4 + 29y^2z^2 - 10z^4)}{44} \\ & - \frac{\sqrt{33}G_{xzz}(4x^4 + 15x^2y^2 - 13x^2z^2 + 11y^4 - 27y^2z^2 + 4z^4)}{44} + \frac{7\sqrt{33}G_{yzyxz}(x^2 + y^2 - 2z^2)}{44} \\ & \frac{3\sqrt{11}G_{uy}(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{88} + \frac{\sqrt{33}G_vy(13x^4 + 12x^2y^2 - 114x^2z^2 - y^4 - 2y^2z^2 + 20z^4)}{88} \\ & - \frac{\sqrt{33}G_{xyx}(3x^4 - x^2y^2 - 29x^2z^2 - 4y^4 + 27y^2z^2 + 10z^4)}{44} + \frac{7\sqrt{33}G_{xzyxz}(x^2 + y^2 - 2z^2)}{44} \\ & - \frac{\sqrt{33}G_{yzz}(11x^4 + 15x^2y^2 - 27x^2z^2 + 4y^4 - 13y^2z^2 + 4z^4)}{44} \end{aligned}$$

$$\bar{Q}_{4,1}^{(2,-1)}[g](E_2, 1), \bar{Q}_{4,2}^{(2,-1)}[g](E_2, 1)$$

** symmetry

$$\frac{\sqrt{35}(x^2 - 2xy - y^2)(x^2 + 2xy - y^2)}{8}$$

$$\frac{\sqrt{35}xy(x - y)(x + y)}{2}$$

** expression

$$\begin{aligned} & \sqrt{3}G_vxyz + \frac{\sqrt{3}G_{xyy}(x - y)(x + y)}{2} - \frac{\sqrt{3}G_{xzy}(3x^2 - y^2)}{4} - \frac{\sqrt{3}G_{yzy}(x^2 - 3y^2)}{4} \\ & - \frac{\sqrt{3}G_vz(x - y)(x + y)}{2} + \sqrt{3}G_{xyxyz} + \frac{\sqrt{3}G_{xzx}(x^2 - 3y^2)}{4} - \frac{\sqrt{3}G_{yzy}(3x^2 - y^2)}{4} \end{aligned}$$

$$\bar{Q}_{4,1}^{(2,-1)}[g](E_2, 2), \bar{Q}_{4,2}^{(2,-1)}[g](E_2, 2)$$

** symmetry

$$-\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

$$\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

** expression

$$-\frac{6\sqrt{7}G_uxyz}{7} - \frac{\sqrt{21}G_{xy}z(3x^2+3y^2-2z^2)}{14} + \frac{\sqrt{21}G_{xz}y(2x^2-y^2+z^2)}{14} - \frac{\sqrt{21}G_{yz}x(x^2-2y^2-z^2)}{14}$$

$$-\frac{3\sqrt{7}G_uz(x-y)(x+y)}{7} - \frac{\sqrt{21}G_vz(3x^2+3y^2-2z^2)}{14} + \frac{\sqrt{21}G_{xx}x(x^2-5y^2+2z^2)}{28} + \frac{\sqrt{21}G_{yy}y(5x^2-y^2-2z^2)}{28}$$

$$\bar{Q}_{4,1}^{(2,1)}[g](E_2, 1), \bar{Q}_{4,2}^{(2,1)}[g](E_2, 1)$$

** symmetry

$$\frac{\sqrt{35}(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}$$

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

** expression

$$-\frac{9\sqrt{154}G_uxyz(x-y)(x+y)}{22} + \frac{\sqrt{462}G_vxyz(x^2+y^2-2z^2)}{44} + \frac{\sqrt{462}G_{xy}z(x-y)(x+y)(x^2+y^2-2z^2)}{88}$$

$$-\frac{\sqrt{462}G_{xz}y(9x^4-14x^2y^2-12x^2z^2+y^4+4y^2z^2)}{88} + \frac{\sqrt{462}G_{yz}x(x^4-14x^2y^2+4x^2z^2+9y^4-12y^2z^2)}{88}$$

$$\frac{9\sqrt{154}G_uz(x^2-2xy-y^2)(x^2+2xy-y^2)}{88} - \frac{\sqrt{462}G_vz(x-y)(x+y)(x^2+y^2-2z^2)}{88} + \frac{\sqrt{462}G_{xy}xyz(x^2+y^2-2z^2)}{44}$$

$$+ \frac{\sqrt{462}G_{xz}x(x^4-8x^2y^2-2x^2z^2+3y^4+6y^2z^2)}{44} + \frac{\sqrt{462}G_{yz}y(3x^4-8x^2y^2+6x^2z^2+y^4-2y^2z^2)}{44}$$

$$\bar{Q}_{4,1}^{(2,1)}[g](E_2, 2), \bar{Q}_{4,2}^{(2,1)}[g](E_2, 2)$$

** symmetry

$$-\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

$$\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

** expression

$$\frac{21\sqrt{22}G_uxyz(x^2+y^2-2z^2)}{44} + \frac{21\sqrt{66}G_vxyz(x-y)(x+y)}{44} - \frac{\sqrt{66}G_{xy}z(9x^4-24x^2y^2-10x^2z^2+9y^4-10y^2z^2+2z^4)}{44}$$

$$+ \frac{\sqrt{66}G_{xz}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44} + \frac{\sqrt{66}G_{yz}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44}$$

$$\frac{21\sqrt{22}G_uz(x-y)(x+y)(x^2+y^2-2z^2)}{88} + \frac{\sqrt{66}G_vz(3x^4-78x^2y^2+20x^2z^2+3y^4+20y^2z^2-4z^4)}{88} + \frac{21\sqrt{66}G_{xy}xyz(x-y)(x+y)}{44}$$

$$+ \frac{\sqrt{66}G_{xz}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44} - \frac{\sqrt{66}G_{yz}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44}$$