

SG No. 121  $D_{2d}^{11}$   $I\bar{4}2m$  [ tetragonal ]

\* plus set:  $+ [0, 0, 0]$ ,  $+ [\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$

\* Wyckoff site: **2a**, site symmetry:  $-42m$

Table 1: Wyckoff bond: **2a@2a**

No.	vector	center	mapping
1	$[0, 0, Z]$	$[0, 0, 0]$	$[1, 2, -3, -4, -5, -6, 7, 8]$

Table 2: Wyckoff bond: **4b@2a**

No.	vector	center	mapping
1	$[X, 0, 0]$	$[0, 0, 0]$	$[1, -2, -5, 6]$
2	$[0, -X, 0]$	$[0, 0, 0]$	$[3, -4, 7, -8]$

Table 3: Wyckoff bond: **4c@2a**

No.	vector	center	mapping
1	$[X, X, 0]$	$[0, 0, 0]$	$[1, -2, -7, 8]$
2	$[X, -X, 0]$	$[0, 0, 0]$	$[3, -4, -5, 6]$

Table 4: Wyckoff bond: **8d@2a**

No.	vector	center	mapping
1	$[X, 0, Z]$	$[0, 0, 0]$	$[1, -5]$
2	$[-X, 0, Z]$	$[0, 0, 0]$	$[2, -6]$
3	$[0, -X, -Z]$	$[0, 0, 0]$	$[3, -8]$
4	$[0, X, -Z]$	$[0, 0, 0]$	$[4, -7]$

Table 5: Wyckoff bond: **8e@2a**

No.	vector	center	mapping
1	$[X, X, Z]$	$[0, 0, 0]$	$[1, 8]$
2	$[-X, -X, Z]$	$[0, 0, 0]$	$[2, 7]$
3	$[X, -X, -Z]$	$[0, 0, 0]$	$[3, 6]$
4	$[-X, X, -Z]$	$[0, 0, 0]$	$[4, 5]$

Table 6: Wyckoff bond: 8f@2a

No.	vector	center	mapping
1	$[X, Y, 0]$	$[0, 0, 0]$	$[1, -2]$
2	$[Y, -X, 0]$	$[0, 0, 0]$	$[3, -4]$
3	$[-X, Y, 0]$	$[0, 0, 0]$	$[5, -6]$
4	$[-Y, -X, 0]$	$[0, 0, 0]$	$[7, -8]$

Table 7: Wyckoff bond: 16g@2a

No.	vector	center	mapping
1	$[X, Y, Z]$	$[0, 0, 0]$	$[1]$
2	$[-X, -Y, Z]$	$[0, 0, 0]$	$[2]$
3	$[Y, -X, -Z]$	$[0, 0, 0]$	$[3]$
4	$[-Y, X, -Z]$	$[0, 0, 0]$	$[4]$
5	$[-X, Y, -Z]$	$[0, 0, 0]$	$[5]$
6	$[X, -Y, -Z]$	$[0, 0, 0]$	$[6]$
7	$[-Y, -X, Z]$	$[0, 0, 0]$	$[7]$
8	$[Y, X, Z]$	$[0, 0, 0]$	$[8]$

\* Wyckoff site: 2b, site symmetry:  $-42m$

Table 8: Wyckoff bond: 2a@2b

No.	vector	center	mapping
1	$[0, 0, Z]$	$[0, 0, \frac{1}{2}]$	$[1, 2, -3, -4, -5, -6, 7, 8]$

Table 9: Wyckoff bond: 4b@2b

No.	vector	center	mapping
1	$[X, 0, 0]$	$[0, 0, \frac{1}{2}]$	$[1, -2, -5, 6]$
2	$[0, -X, 0]$	$[0, 0, \frac{1}{2}]$	$[3, -4, 7, -8]$

Table 10: Wyckoff bond: 4c@2b

No.	vector	center	mapping
1	$[X, X, 0]$	$[0, 0, \frac{1}{2}]$	$[1, -2, -7, 8]$
2	$[X, -X, 0]$	$[0, 0, \frac{1}{2}]$	$[3, -4, -5, 6]$

Table 11: Wyckoff bond: **8d@2b**

No.	vector	center	mapping
1	$[X, 0, Z]$	$[0, 0, \frac{1}{2}]$	$[1, -5]$
2	$[-X, 0, Z]$	$[0, 0, \frac{1}{2}]$	$[2, -6]$
3	$[0, -X, -Z]$	$[0, 0, \frac{1}{2}]$	$[3, -8]$
4	$[0, X, -Z]$	$[0, 0, \frac{1}{2}]$	$[4, -7]$

Table 12: Wyckoff bond: **8e@2b**

No.	vector	center	mapping
1	$[X, X, Z]$	$[0, 0, \frac{1}{2}]$	$[1, 8]$
2	$[-X, -X, Z]$	$[0, 0, \frac{1}{2}]$	$[2, 7]$
3	$[X, -X, -Z]$	$[0, 0, \frac{1}{2}]$	$[3, 6]$
4	$[-X, X, -Z]$	$[0, 0, \frac{1}{2}]$	$[4, 5]$

Table 13: Wyckoff bond: **8f@2b**

No.	vector	center	mapping
1	$[X, Y, 0]$	$[0, 0, \frac{1}{2}]$	$[1, -2]$
2	$[Y, -X, 0]$	$[0, 0, \frac{1}{2}]$	$[3, -4]$
3	$[-X, Y, 0]$	$[0, 0, \frac{1}{2}]$	$[5, -6]$
4	$[-Y, -X, 0]$	$[0, 0, \frac{1}{2}]$	$[7, -8]$

Table 14: Wyckoff bond: **16g@2b**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[0, 0, \frac{1}{2}]$	$[1]$
2	$[-X, -Y, Z]$	$[0, 0, \frac{1}{2}]$	$[2]$
3	$[Y, -X, -Z]$	$[0, 0, \frac{1}{2}]$	$[3]$
4	$[-Y, X, -Z]$	$[0, 0, \frac{1}{2}]$	$[4]$
5	$[-X, Y, -Z]$	$[0, 0, \frac{1}{2}]$	$[5]$
6	$[X, -Y, -Z]$	$[0, 0, \frac{1}{2}]$	$[6]$
7	$[-Y, -X, Z]$	$[0, 0, \frac{1}{2}]$	$[7]$
8	$[Y, X, Z]$	$[0, 0, \frac{1}{2}]$	$[8]$

\* Wyckoff site: **4c**, site symmetry: **222**.

Table 15: Wyckoff bond: 4a@4c

No.	vector	center	mapping
1	$[X, 0, 0]$	$[0, \frac{1}{2}, 0]$	$[1, -2, -5, 6]$
2	$[0, -X, 0]$	$[\frac{1}{2}, 0, 0]$	$[3, -4, 7, -8]$

Table 16: Wyckoff bond: 4b@4c

No.	vector	center	mapping
1	$[0, X, 0]$	$[0, \frac{1}{2}, 0]$	$[1, -2, 5, -6]$
2	$[X, 0, 0]$	$[\frac{1}{2}, 0, 0]$	$[3, -4, -7, 8]$

Table 17: Wyckoff bond: 4c@4c

No.	vector	center	mapping
1	$[0, 0, Z]$	$[0, \frac{1}{2}, 0]$	$[1, 2, -5, -6]$
2	$[0, 0, -Z]$	$[\frac{1}{2}, 0, 0]$	$[3, 4, -7, -8]$

Table 18: Wyckoff bond: 8d@4c

No.	vector	center	mapping
1	$[X, 0, Z]$	$[0, \frac{1}{2}, 0]$	$[1, -5]$
2	$[-X, 0, Z]$	$[0, \frac{1}{2}, 0]$	$[2, -6]$
3	$[0, -X, -Z]$	$[\frac{1}{2}, 0, 0]$	$[3, -8]$
4	$[0, X, -Z]$	$[\frac{1}{2}, 0, 0]$	$[4, -7]$

Table 19: Wyckoff bond: 8e@4c

No.	vector	center	mapping
1	$[0, X, Z]$	$[0, \frac{1}{2}, 0]$	$[1, -6]$
2	$[0, -X, Z]$	$[0, \frac{1}{2}, 0]$	$[2, -5]$
3	$[X, 0, -Z]$	$[\frac{1}{2}, 0, 0]$	$[3, -7]$
4	$[-X, 0, -Z]$	$[\frac{1}{2}, 0, 0]$	$[4, -8]$

Table 20: Wyckoff bond: **8f@4c**

No.	vector	center	mapping
1	$[X, Y, 0]$	$[0, \frac{1}{2}, 0]$	$[1, -2]$
2	$[Y, -X, 0]$	$[\frac{1}{2}, 0, 0]$	$[3, -4]$
3	$[-X, Y, 0]$	$[0, \frac{1}{2}, 0]$	$[5, -6]$
4	$[-Y, -X, 0]$	$[\frac{1}{2}, 0, 0]$	$[7, -8]$

Table 21: Wyckoff bond: **16g@4c**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[0, \frac{1}{2}, 0]$	$[1]$
2	$[-X, -Y, Z]$	$[0, \frac{1}{2}, 0]$	$[2]$
3	$[Y, -X, -Z]$	$[\frac{1}{2}, 0, 0]$	$[3]$
4	$[-Y, X, -Z]$	$[\frac{1}{2}, 0, 0]$	$[4]$
5	$[-X, Y, -Z]$	$[0, \frac{1}{2}, 0]$	$[5]$
6	$[X, -Y, -Z]$	$[0, \frac{1}{2}, 0]$	$[6]$
7	$[-Y, -X, Z]$	$[\frac{1}{2}, 0, 0]$	$[7]$
8	$[Y, X, Z]$	$[\frac{1}{2}, 0, 0]$	$[8]$

\* Wyckoff site: **4d**, site symmetry:  $-4..$

Table 22: Wyckoff bond: **4a@4d**

No.	vector	center	mapping
1	$[0, 0, Z]$	$[0, \frac{1}{2}, \frac{1}{4}]$	$[1, 2, -3, -4]$
2	$[0, 0, -Z]$	$[0, \frac{1}{2}, \frac{3}{4}]$	$[5, 6, -7, -8]$

Table 23: Wyckoff bond: **8b@4d**

No.	vector	center	mapping
1	$[X, Y, 0]$	$[0, \frac{1}{2}, \frac{1}{4}]$	$[1, -2]$
2	$[Y, -X, 0]$	$[0, \frac{1}{2}, \frac{1}{4}]$	$[3, -4]$
3	$[-X, Y, 0]$	$[0, \frac{1}{2}, \frac{3}{4}]$	$[5, -6]$
4	$[-Y, -X, 0]$	$[0, \frac{1}{2}, \frac{3}{4}]$	$[7, -8]$

Table 24: Wyckoff bond: **16c@4d**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[0, \frac{1}{2}, \frac{1}{4}]$	$[1]$

*continued ...*

Table 24

No.	vector	center	mapping
2	$[-X, -Y, Z]$	$[0, \frac{1}{2}, \frac{1}{4}]$	[2]
3	$[Y, -X, -Z]$	$[0, \frac{1}{2}, \frac{1}{4}]$	[3]
4	$[-Y, X, -Z]$	$[0, \frac{1}{2}, \frac{1}{4}]$	[4]
5	$[-X, Y, -Z]$	$[0, \frac{1}{2}, \frac{3}{4}]$	[5]
6	$[X, -Y, -Z]$	$[0, \frac{1}{2}, \frac{3}{4}]$	[6]
7	$[-Y, -X, Z]$	$[0, \frac{1}{2}, \frac{3}{4}]$	[7]
8	$[Y, X, Z]$	$[0, \frac{1}{2}, \frac{3}{4}]$	[8]

\* Wyckoff site:  $4e$ , site symmetry:  $2.mm$

Table 25: Wyckoff bond:  $4a@4e$ 

No.	vector	center	mapping
1	$[X, X, 0]$	$[0, 0, z]$	[1,-2,-7,8]
2	$[X, -X, 0]$	$[0, 0, -z]$	[3,-4,-5,6]

Table 26: Wyckoff bond:  $4b@4e$ 

No.	vector	center	mapping
1	$[0, 0, Z]$	$[0, 0, z]$	[1,2,7,8]
2	$[0, 0, -Z]$	$[0, 0, -z]$	[3,4,5,6]

Table 27: Wyckoff bond:  $8c@4e$ 

No.	vector	center	mapping
1	$[X, X, Z]$	$[0, 0, z]$	[1,8]
2	$[-X, -X, Z]$	$[0, 0, z]$	[2,7]
3	$[X, -X, -Z]$	$[0, 0, -z]$	[3,6]
4	$[-X, X, -Z]$	$[0, 0, -z]$	[4,5]

Table 28: Wyckoff bond:  $8d@4e$ 

No.	vector	center	mapping
1	$[X, Y, 0]$	$[0, 0, z]$	[1,-2]
2	$[Y, -X, 0]$	$[0, 0, -z]$	[3,-4]
3	$[-X, Y, 0]$	$[0, 0, -z]$	[5,-6]
4	$[-Y, -X, 0]$	$[0, 0, z]$	[7,-8]

Table 29: Wyckoff bond: **16e@4e**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[0, 0, z]$	[1]
2	$[-X, -Y, Z]$	$[0, 0, z]$	[2]
3	$[Y, -X, -Z]$	$[0, 0, -z]$	[3]
4	$[-Y, X, -Z]$	$[0, 0, -z]$	[4]
5	$[-X, Y, -Z]$	$[0, 0, -z]$	[5]
6	$[X, -Y, -Z]$	$[0, 0, -z]$	[6]
7	$[-Y, -X, Z]$	$[0, 0, z]$	[7]
8	$[Y, X, Z]$	$[0, 0, z]$	[8]

\* Wyckoff site: **8f**, site symmetry:  $.2$ .

Table 30: Wyckoff bond: **8a@8f**

No.	vector	center	mapping
1	$[0, X, Z]$	$[x, 0, 0]$	[1,-6]
2	$[0, -X, Z]$	$[-x, 0, 0]$	[2,-5]
3	$[X, 0, -Z]$	$[0, -x, 0]$	[3,-7]
4	$[-X, 0, -Z]$	$[0, x, 0]$	[4,-8]

Table 31: Wyckoff bond: **8b@8f**

No.	vector	center	mapping
1	$[X, 0, 0]$	$[x, 0, 0]$	[1,6]
2	$[-X, 0, 0]$	$[-x, 0, 0]$	[2,5]
3	$[0, -X, 0]$	$[0, -x, 0]$	[3,7]
4	$[0, X, 0]$	$[0, x, 0]$	[4,8]

Table 32: Wyckoff bond: **16c@8f**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[x, 0, 0]$	[1]
2	$[-X, -Y, Z]$	$[-x, 0, 0]$	[2]
3	$[Y, -X, -Z]$	$[0, -x, 0]$	[3]
4	$[-Y, X, -Z]$	$[0, x, 0]$	[4]
5	$[-X, Y, -Z]$	$[-x, 0, 0]$	[5]
6	$[X, -Y, -Z]$	$[x, 0, 0]$	[6]
7	$[-Y, -X, Z]$	$[0, -x, 0]$	[7]
8	$[Y, X, Z]$	$[0, x, 0]$	[8]

\* Wyckoff site: **8g**, site symmetry:  $.2$ .

Table 33: Wyckoff bond: **8a@8g**

No.	vector	center	mapping
1	$[0, X, Z]$	$[x, 0, \frac{1}{2}]$	$[1, -6]$
2	$[0, -X, Z]$	$[-x, 0, \frac{1}{2}]$	$[2, -5]$
3	$[X, 0, -Z]$	$[0, -x, \frac{1}{2}]$	$[3, -7]$
4	$[-X, 0, -Z]$	$[0, x, \frac{1}{2}]$	$[4, -8]$

Table 34: Wyckoff bond: **8b@8g**

No.	vector	center	mapping
1	$[X, 0, 0]$	$[x, 0, \frac{1}{2}]$	$[1, 6]$
2	$[-X, 0, 0]$	$[-x, 0, \frac{1}{2}]$	$[2, 5]$
3	$[0, -X, 0]$	$[0, -x, \frac{1}{2}]$	$[3, 7]$
4	$[0, X, 0]$	$[0, x, \frac{1}{2}]$	$[4, 8]$

Table 35: Wyckoff bond: **16c@8g**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[x, 0, \frac{1}{2}]$	$[1]$
2	$[-X, -Y, Z]$	$[-x, 0, \frac{1}{2}]$	$[2]$
3	$[Y, -X, -Z]$	$[0, -x, \frac{1}{2}]$	$[3]$
4	$[-Y, X, -Z]$	$[0, x, \frac{1}{2}]$	$[4]$
5	$[-X, Y, -Z]$	$[-x, 0, \frac{1}{2}]$	$[5]$
6	$[X, -Y, -Z]$	$[x, 0, \frac{1}{2}]$	$[6]$
7	$[-Y, -X, Z]$	$[0, -x, \frac{1}{2}]$	$[7]$
8	$[Y, X, Z]$	$[0, x, \frac{1}{2}]$	$[8]$

\* Wyckoff site: **8h**, site symmetry:  $2..$

Table 36: Wyckoff bond: **8a@8h**

No.	vector	center	mapping
1	$[X, Y, 0]$	$[0, \frac{1}{2}, z]$	$[1, -2]$
2	$[Y, -X, 0]$	$[\frac{1}{2}, 0, -z]$	$[3, -4]$
3	$[-X, Y, 0]$	$[0, \frac{1}{2}, -z]$	$[5, -6]$
4	$[-Y, -X, 0]$	$[\frac{1}{2}, 0, z]$	$[7, -8]$

Table 37: Wyckoff bond: **8b@8h**

No.	vector	center	mapping
1	$[0, 0, Z]$	$[0, \frac{1}{2}, z]$	[1, 2]
2	$[0, 0, -Z]$	$[\frac{1}{2}, 0, -z]$	[3, 4]
3	$[0, 0, -Z]$	$[0, \frac{1}{2}, -z]$	[5, 6]
4	$[0, 0, Z]$	$[\frac{1}{2}, 0, z]$	[7, 8]

Table 38: Wyckoff bond: **16c@8h**

No.	vector	center	mapping
1	$[X, Y, Z]$	$[0, \frac{1}{2}, z]$	[1]
2	$[-X, -Y, Z]$	$[0, \frac{1}{2}, z]$	[2]
3	$[Y, -X, -Z]$	$[\frac{1}{2}, 0, -z]$	[3]
4	$[-Y, X, -Z]$	$[\frac{1}{2}, 0, -z]$	[4]
5	$[-X, Y, -Z]$	$[0, \frac{1}{2}, -z]$	[5]
6	$[X, -Y, -Z]$	$[0, \frac{1}{2}, -z]$	[6]
7	$[-Y, -X, Z]$	$[\frac{1}{2}, 0, z]$	[7]
8	$[Y, X, Z]$	$[\frac{1}{2}, 0, z]$	[8]

\* Wyckoff site: **8i**, site symmetry:  $\dots m$

Table 39: Wyckoff bond: **8a@8i**

No.	vector	center	mapping
1	$[X, X, Z]$	$[x, x, z]$	[1, 8]
2	$[-X, -X, Z]$	$[-x, -x, z]$	[2, 7]
3	$[X, -X, -Z]$	$[x, -x, -z]$	[3, 6]
4	$[-X, X, -Z]$	$[-x, x, -z]$	[4, 5]

Table 40: Wyckoff bond: **8b@8i**

No.	vector	center	mapping
1	$[X, -X, 0]$	$[x, x, z]$	[1, -8]
2	$[-X, X, 0]$	$[-x, -x, z]$	[2, -7]
3	$[-X, -X, 0]$	$[x, -x, -z]$	[3, -6]
4	$[X, X, 0]$	$[-x, x, -z]$	[4, -5]

Table 41: Wyckoff bond: 16c@8i

No.	vector	center	mapping
1	$[X, Y, Z]$	$[x, x, z]$	[1]
2	$[-X, -Y, Z]$	$[-x, -x, z]$	[2]
3	$[Y, -X, -Z]$	$[x, -x, -z]$	[3]
4	$[-Y, X, -Z]$	$[-x, x, -z]$	[4]
5	$[-X, Y, -Z]$	$[-x, x, -z]$	[5]
6	$[X, -Y, -Z]$	$[x, -x, -z]$	[6]
7	$[-Y, -X, Z]$	$[-x, -x, z]$	[7]
8	$[Y, X, Z]$	$[x, x, z]$	[8]

\* Wyckoff site: 16j, site symmetry: 1

Table 42: Wyckoff bond: 16a@16j

No.	vector	center	mapping
1	$[X, Y, Z]$	$[x, y, z]$	[1]
2	$[-X, -Y, Z]$	$[-x, -y, z]$	[2]
3	$[Y, -X, -Z]$	$[y, -x, -z]$	[3]
4	$[-Y, X, -Z]$	$[-y, x, -z]$	[4]
5	$[-X, Y, -Z]$	$[-x, y, -z]$	[5]
6	$[X, -Y, -Z]$	$[x, -y, -z]$	[6]
7	$[-Y, -X, Z]$	$[-y, -x, z]$	[7]
8	$[Y, X, Z]$	$[y, x, z]$	[8]