

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag                                     | matrix (polar)  | det | TR |
|-----|---|---|-----|----|
| 1   | $\{1 0\}$                               | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                       | 1   | 1  |
| 2   | $\{2_{100} \frac{1}{2}\frac{1}{2}0\}$   | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | 1   | 1  |
| 3   | $\{2_{010} \frac{1}{2}\frac{1}{2}0\}$   | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | 1   | 1  |
| 4   | $\{2_{001} 0\}$                         | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                     | 1   | 1  |
| 5   | $\{-4_{001}^+ 0\}$                      | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                     | -1  | -1 |
| 6   | $\{-4_{001}^- 0\}$                      | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                     | -1  | -1 |
| 7   | $\{m_{110}' \frac{1}{2}\frac{1}{2}0\}$  | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 \end{bmatrix}$ | -1  | -1 |
| 8   | $\{m_{1-10}' \frac{1}{2}\frac{1}{2}0\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 \end{bmatrix}$   | -1  | -1 |