

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag   | matrix (polar)  | det | TR |
|-----|---|---|-----|----|
| 1   | $\{1 0\}$   | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                 | 1   | 1  |
| 2   | $\{4^+_{001} \frac{1}{2}\frac{1}{2}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{4} \end{bmatrix}$  | 1   | 1  |
| 3   | $\{4^-_{001} \frac{1}{2}\frac{1}{2}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{3}{4} \end{bmatrix}$  | 1   | 1  |
| 4   | $\{2_{001} 00\frac{1}{2}\}$                       | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$                     | 1   | 1  |
| 5   | $\{2_{100}' \frac{1}{2}\frac{1}{2}\frac{3}{4}\}$  | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{3}{4} \end{bmatrix}$ | 1   | -1 |
| 6   | $\{2_{010}' \frac{1}{2}\frac{1}{2}\frac{1}{4}\}$  | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{4} \end{bmatrix}$ | 1   | -1 |
| 7   | $\{2_{110}' 0\}$                                  | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                                | 1   | -1 |
| 8   | $\{2_{1-10}' 00\frac{1}{2}\}$                     | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$                    | 1   | -1 |